

For implement the transient heat conduction:

$$\rho c_p \frac{\partial T}{\partial t} + k \frac{\partial^2 T}{\partial x^2} = 0 \quad : \text{ constant } k = 400, \rho = 870, \text{ Cp} = 38.5$$

IC:

$$T_o = 293.15$$

BC:

$$\frac{\partial T}{\partial x} \Big|_{x=0} = 0 \text{ and } \frac{\partial T}{\partial x} \Big|_{x=L} = h(T_\infty - T)$$

Weak Form

$$\int_0^L \nu \cdot \rho c_p \frac{\partial T}{\partial t} dx + \int_0^L \nu \cdot k \frac{\partial^2 T}{\partial x^2} dx = 0$$

Bypart intrigation

$$\int_0^L \nu \cdot \rho c_p \frac{\partial T}{\partial t} dx + \left[\nu \cdot k \frac{\partial T}{\partial x} \right]_0^L - \int_0^L k \frac{\partial \nu}{\partial x} \frac{\partial T}{\partial x} dx = 0$$

$$\int_0^L \left[\nu \cdot \rho c_p \frac{\partial T}{\partial t} + k \frac{\partial \nu}{\partial x} \frac{\partial T}{\partial x} \right] dx + [\nu \cdot h(T_\infty - T)]_L - [0]_0 = 0$$

Domain setting

dweak

T_test*rho*cp*T_time

weak

k*Tx_test*Tx

Boundary setting

point 1

0

point 2

T_test*h*(850-T)