

# **Simulation of chromatographic band transport**

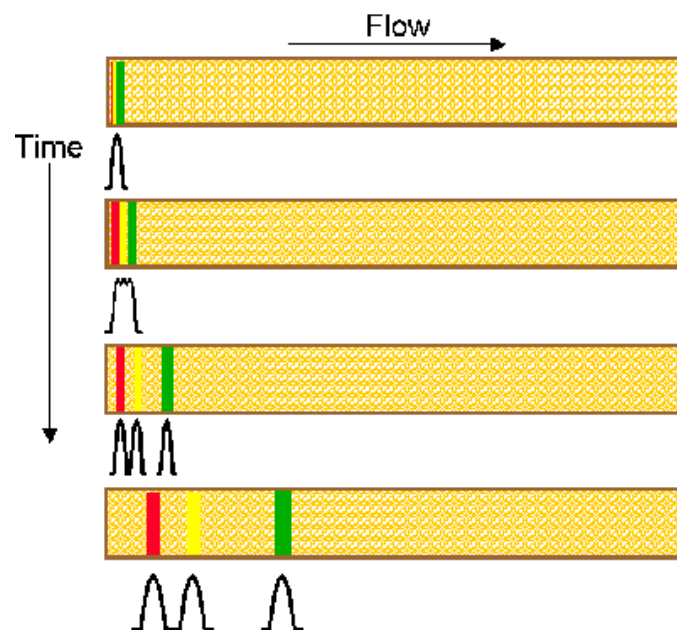
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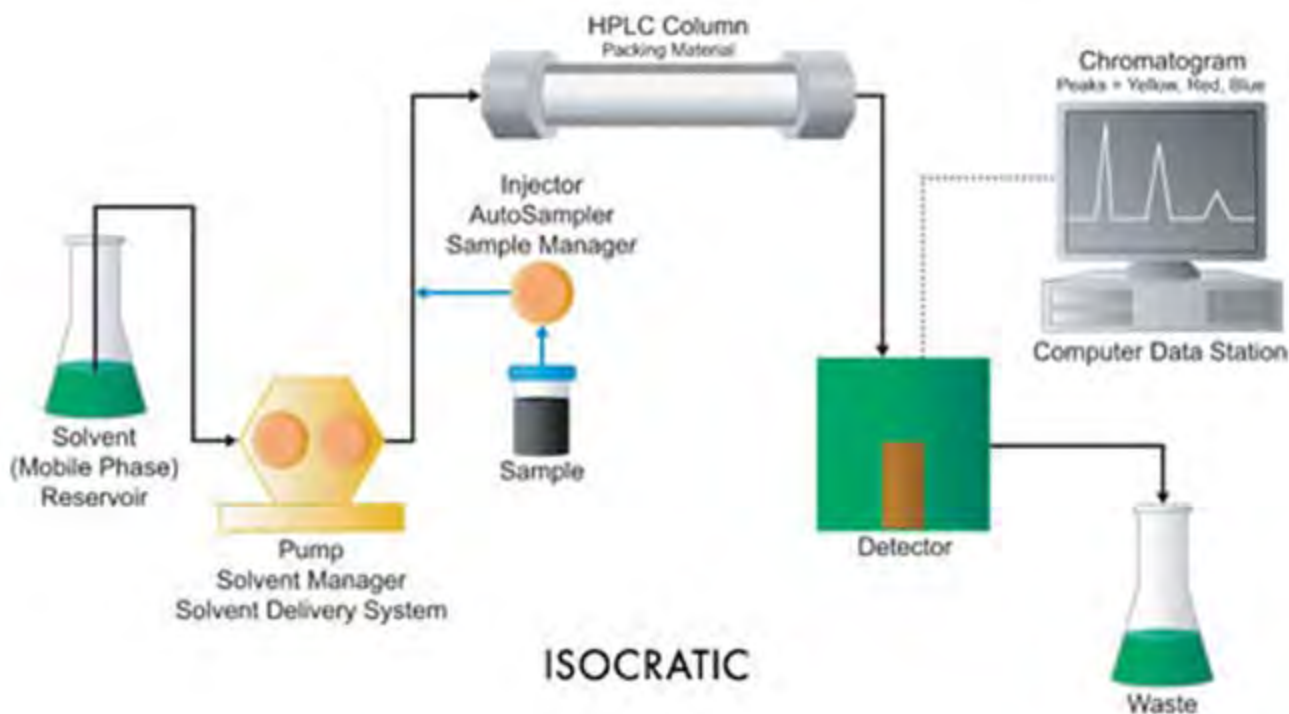
1. About chromatography
2. Detector cell: Band transport in open fluid  
→ Navier-Stokes + convection-diffusion
3. Microfluidic chip: Band transport in a packed bed:  
+ Darcy's law
4. Thermal effects in 2.1 mm column  
+ heat equation

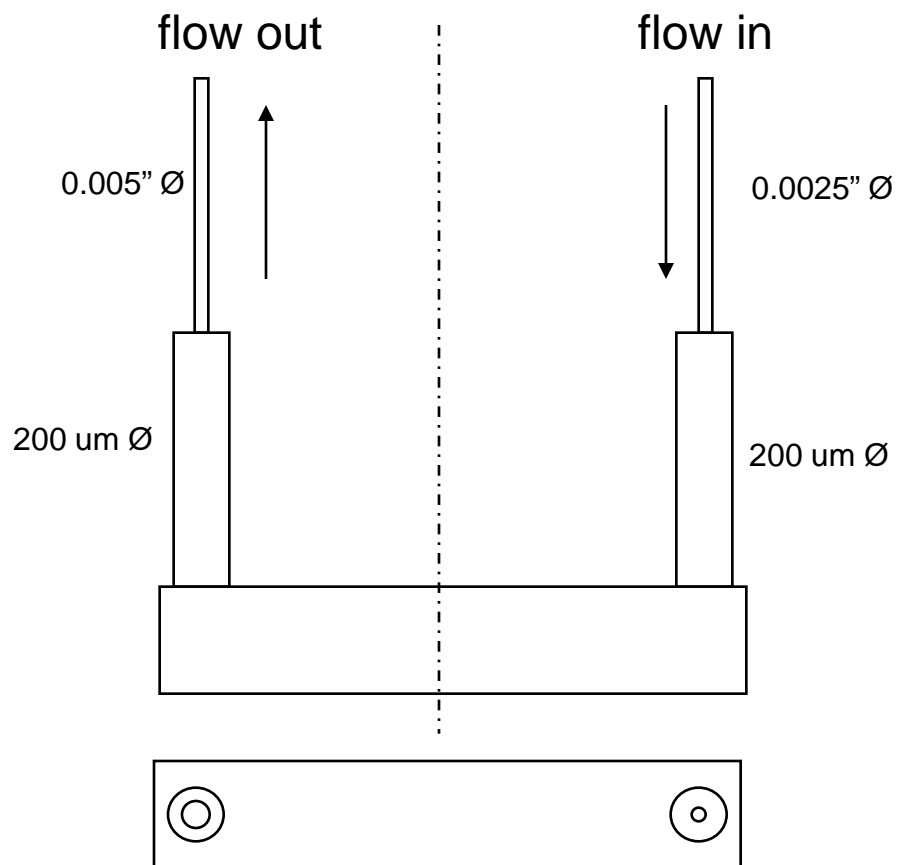
# What is chromatography?

- Pass a mixture of chemical species dissolved in a liquid mobile phase through a stationary phase physically located in a column
- Depending on chemical affinity of the different species with the stationary phase, they elute at different times  $\Rightarrow$  separation

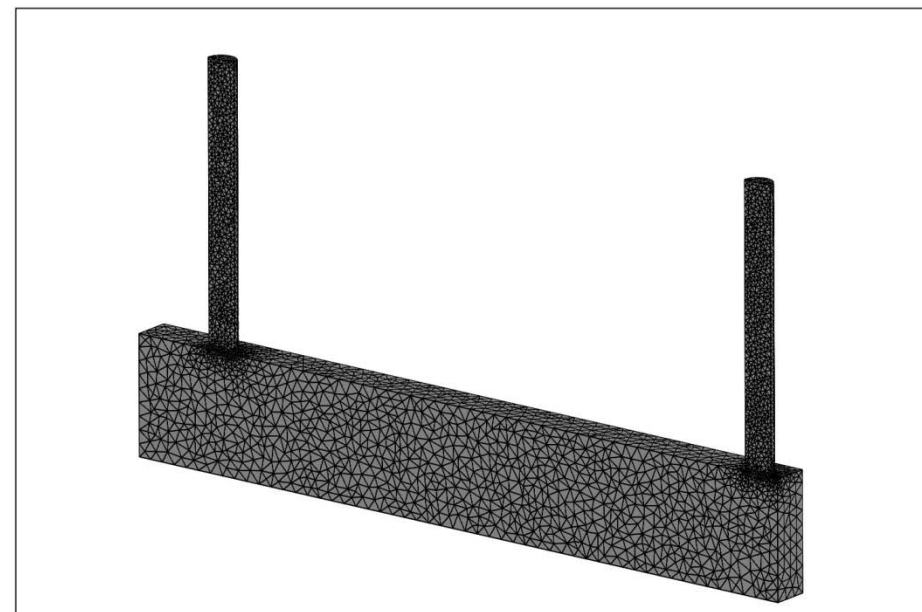


# An HPLC system





**geometry**



**mesh**

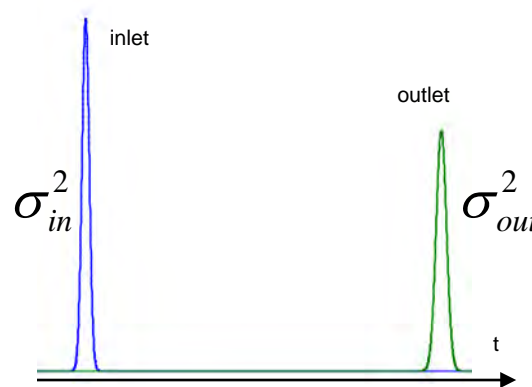
- Incompressible Navier-Stokes

$$\rho \frac{\partial \vec{u}}{\partial t} + \rho \vec{u} \cdot \nabla \vec{u} = \mu \nabla^2 \vec{u}$$

- Convection-diffusion for analyte band

$$\frac{\partial C}{\partial t} + \vec{u} \cdot \nabla C = D \nabla^2 C$$

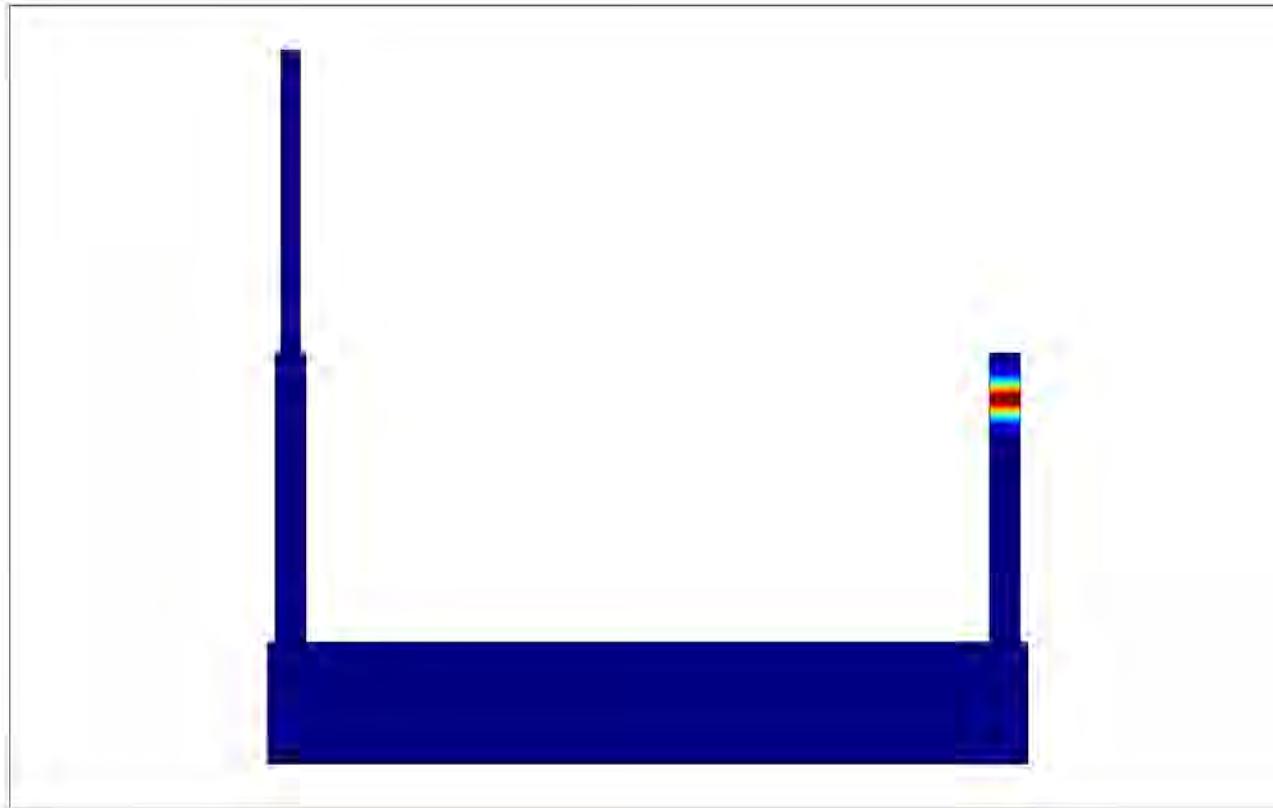
numerical vs physical diffusion



# Velocity field



# Band transport





# Transport in a packed bed

- Solvent: Darcy's law  $\nabla^2 P = 0$

superficial velocity  $\vec{U}_s = -\frac{k}{\mu} \nabla P$

permeability  $k = \frac{d_p^2 \varepsilon^3}{180(1-\varepsilon)^2}$  void fraction  $\varepsilon = \frac{V_m}{V_{tot}}$

- Solute:

linear velocity  $\vec{u} = \frac{\vec{U}_s}{\varepsilon_t}$

evolution of concentration

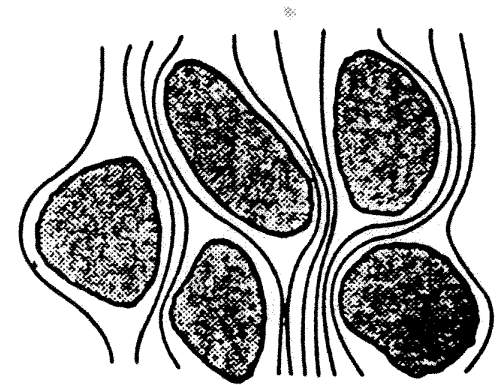
$$\frac{\partial C}{\partial t} + \vec{u} \cdot \nabla C = D_{eff} \nabla^2 C$$

effective diffusion coefficient

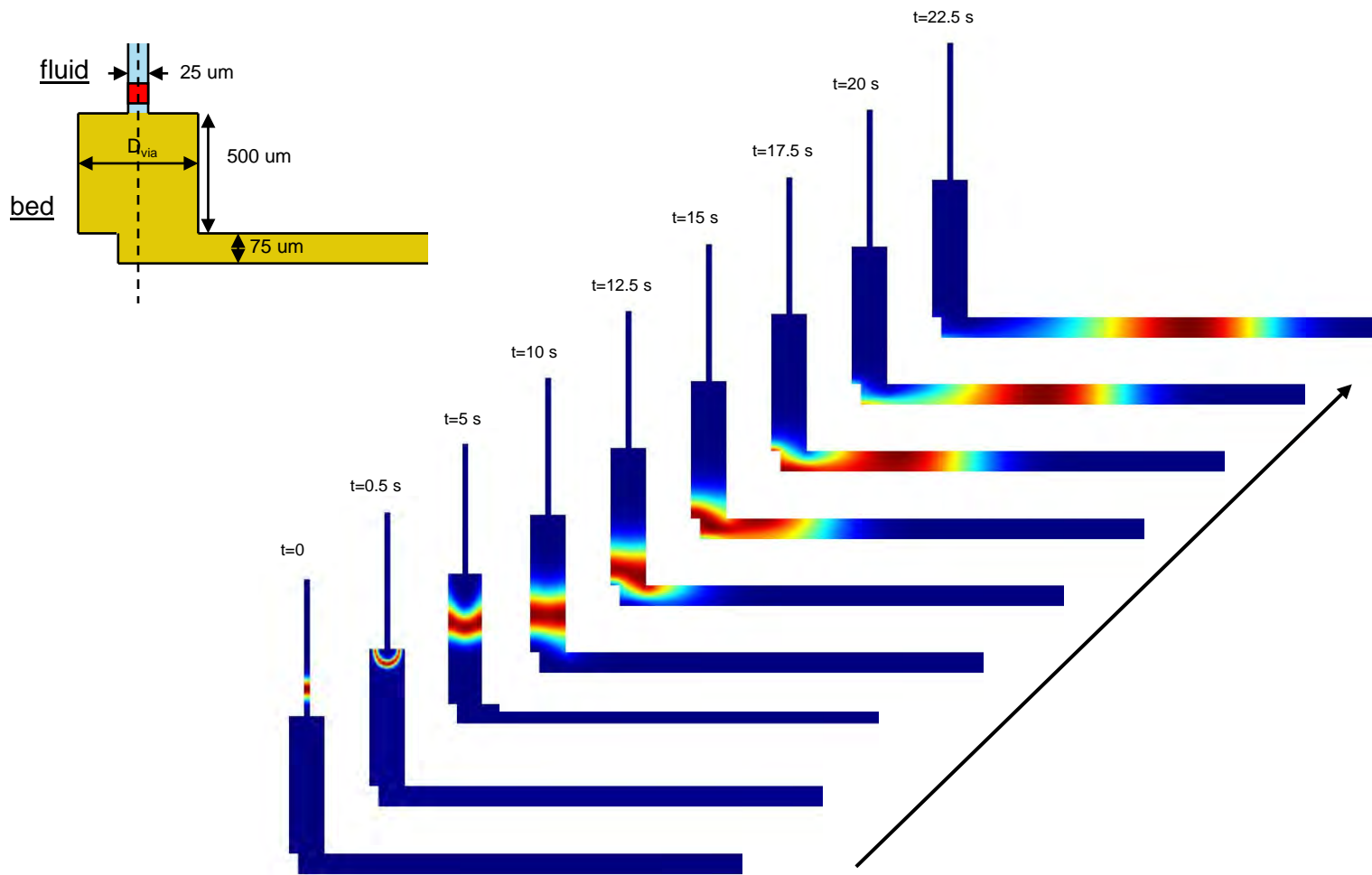
$$D_{eff} = \frac{H u}{2}$$

plate height (Van Deemter)

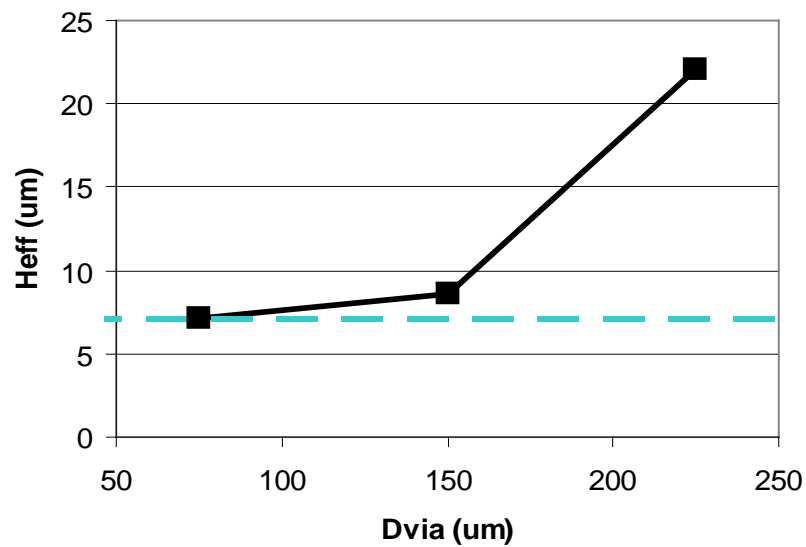
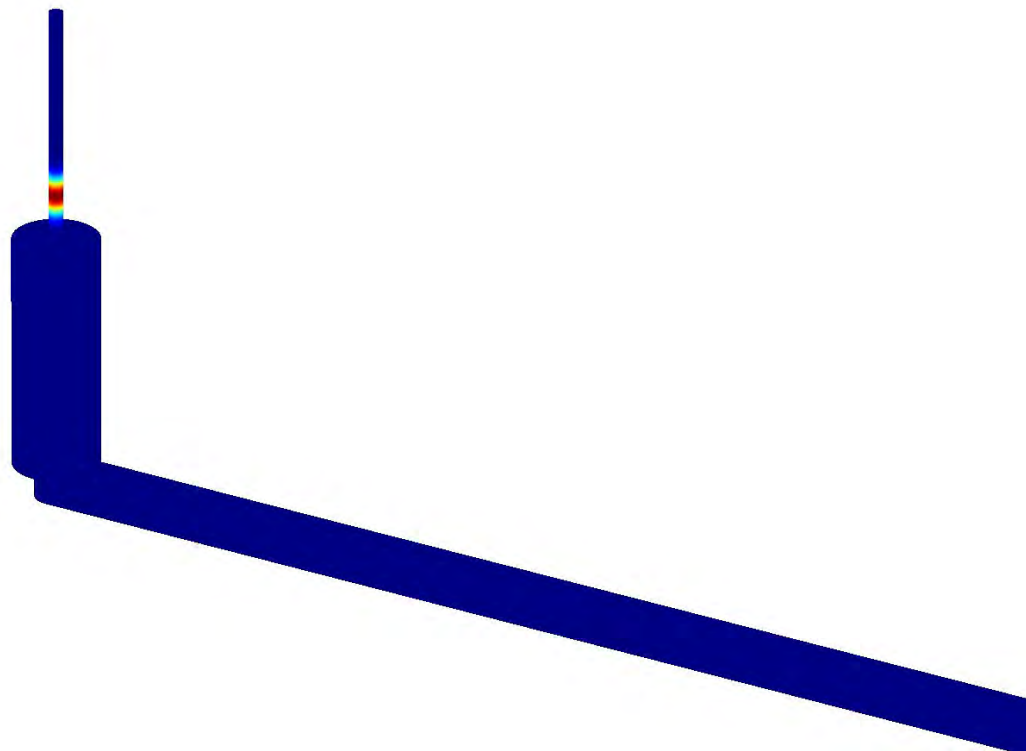
$$H(u) = 1.5 d_p + \frac{D_{mol}}{u} + \frac{d_p^2}{6 D_{mol}} u$$



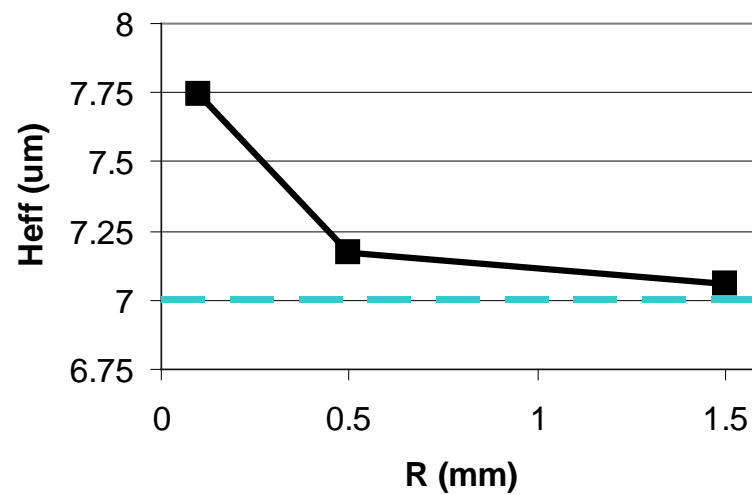
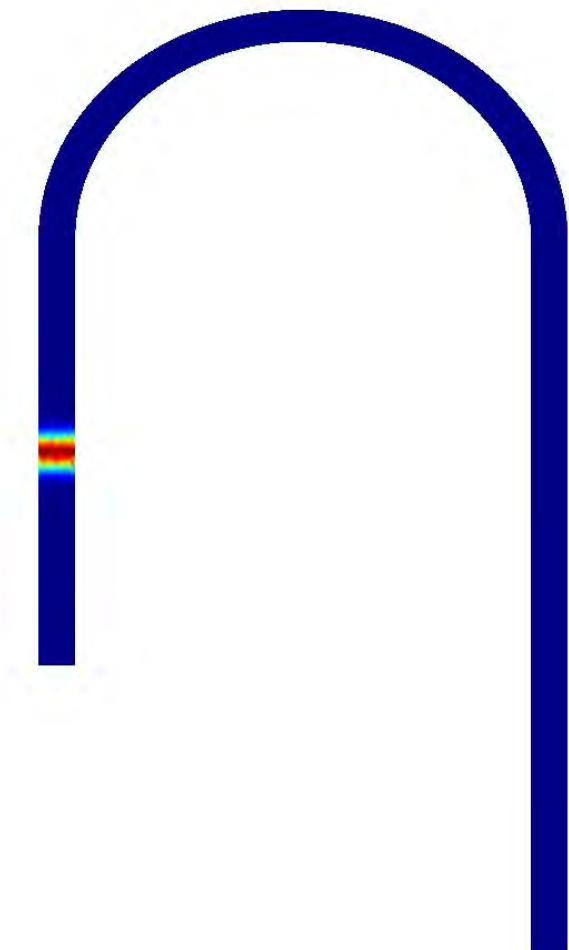
# Microfluidic chip: inlet/outlet vias



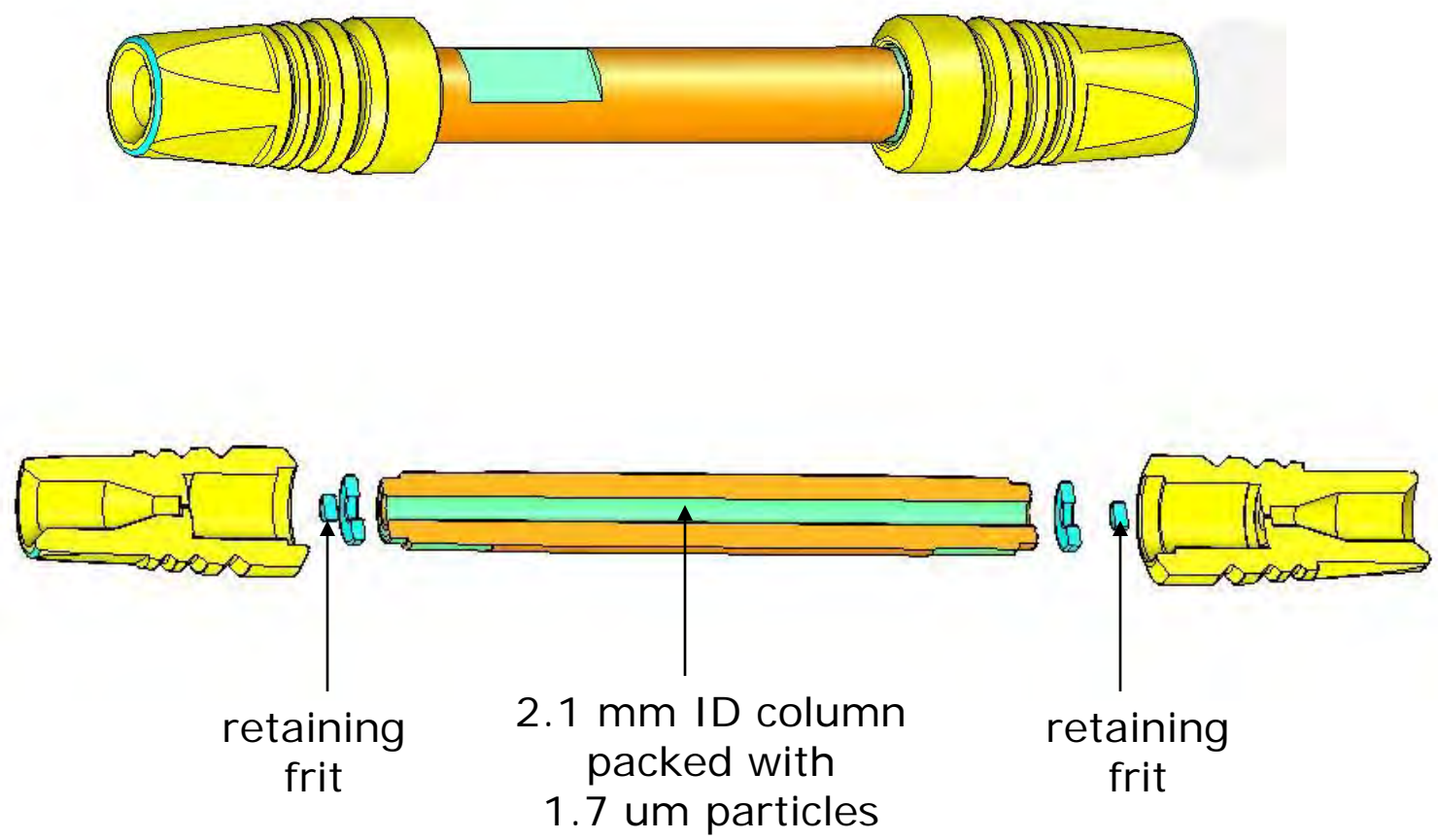
# Microfluidic chip: inlet/outlet vias



# Microfluidic chip: bends

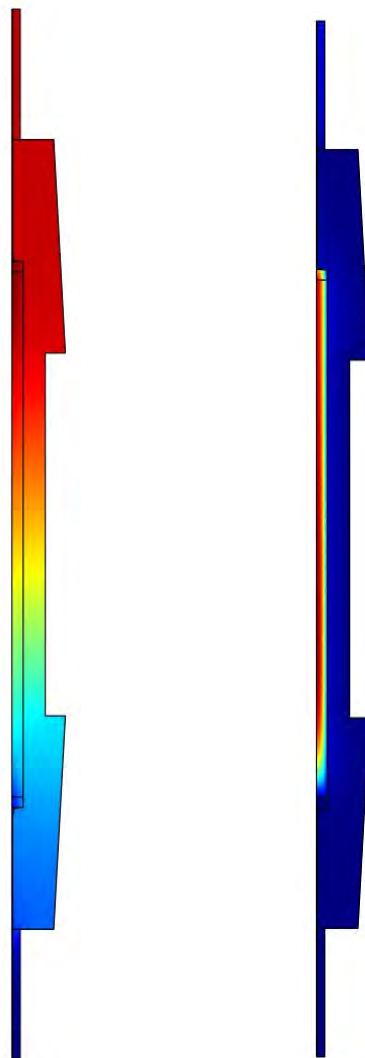
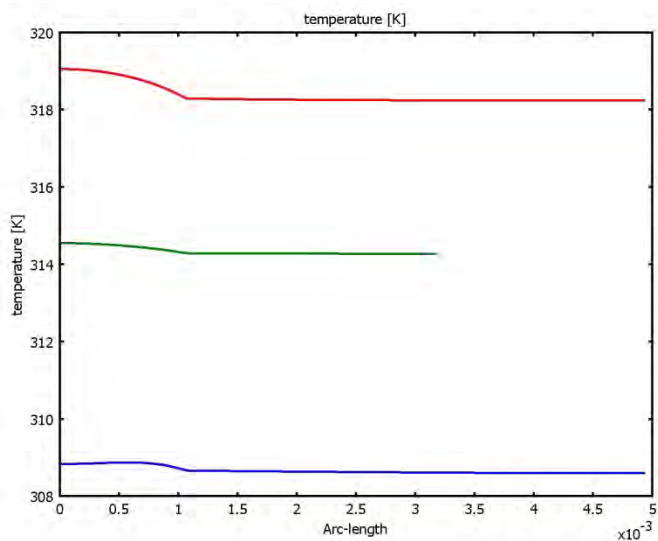


# Thermal effects in 2.1 mm columns



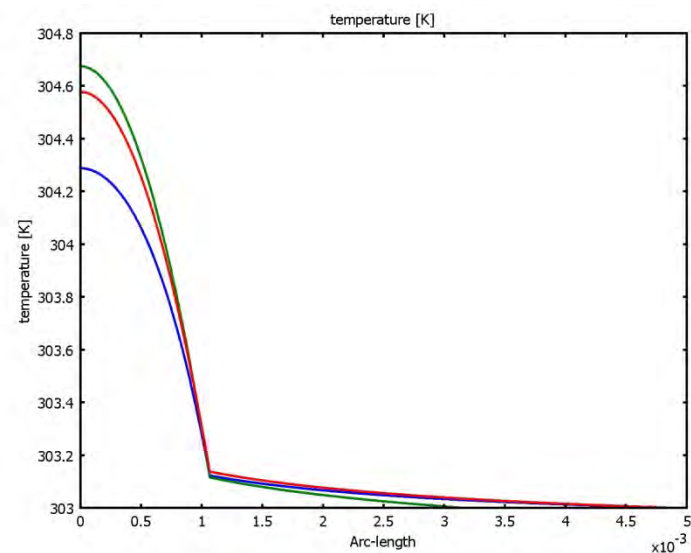
## adiabatic BCs

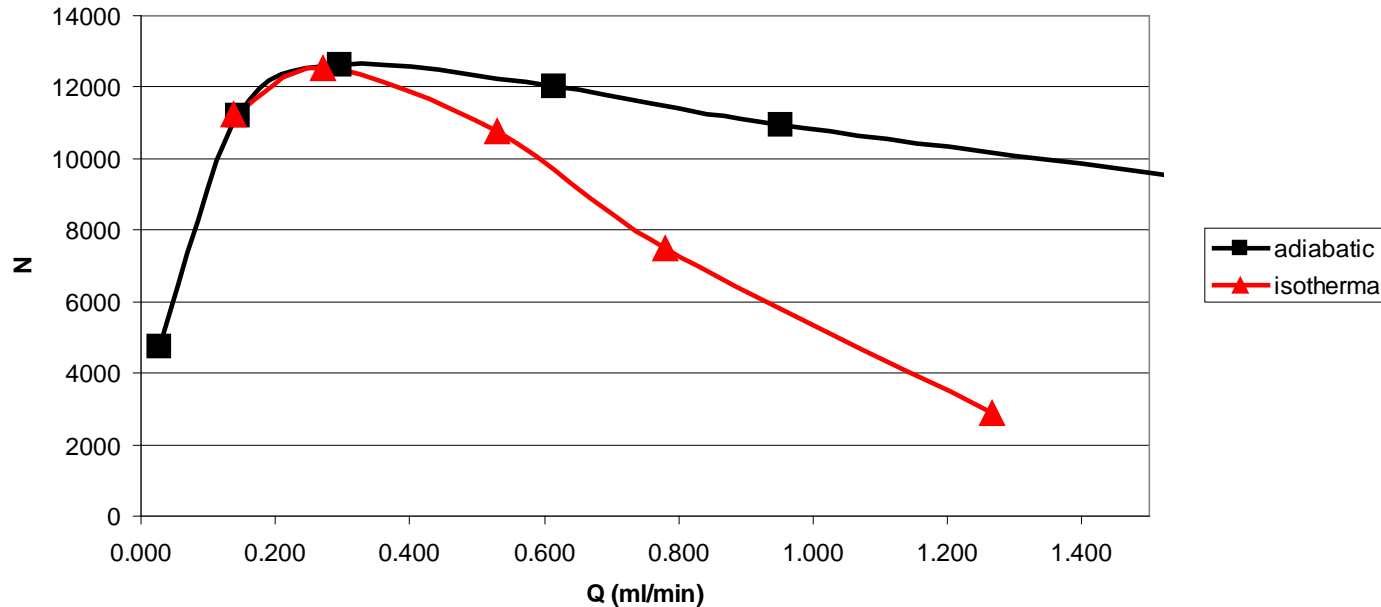
$$\Delta T_{\max} = 16.6 \text{ K}$$



## isothermal BCs

$$\Delta T_{\max} = 1.7 \text{ K}$$





- Heating and the temperature dependence of viscosity and diffusion coefficient can combine to create a significant drop of performance

- Effect of artificial and numerical diffusion in convection-diffusion problems:

