Mapping the Limitations of Breakthrough Analysis in Fixed-Bed Adsorption James Clinton Knox

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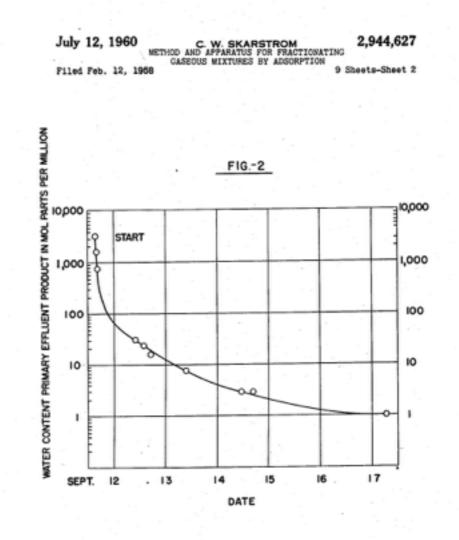
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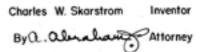
Introduction: Field of Study

- Gas separation processes using fixed beds of adsorbents are important in many existing and emerging industries
- Adsorbent processes are typically cyclic, with adsorption and desorption steps that swing between high and low pressures, temperatures, or concentrations (PSA, TSA, CSA)
- Computer simulations are typically used to select hardware and process parameters (adsorbent type, layer sizes, pressure and temperature set points, cycle time, flow rate, etc.)
- * A cyclic steady-state condition is only reached after many cycles
- * Simulation execution speed is critical due to the large trade space and extensive number of cycles required for a single data point

Skarstrom Patent

- Pressure swing adsorption process
- * Air drying using silica gel beds
- Cyclic steady state only achieved after
 6 days of operation





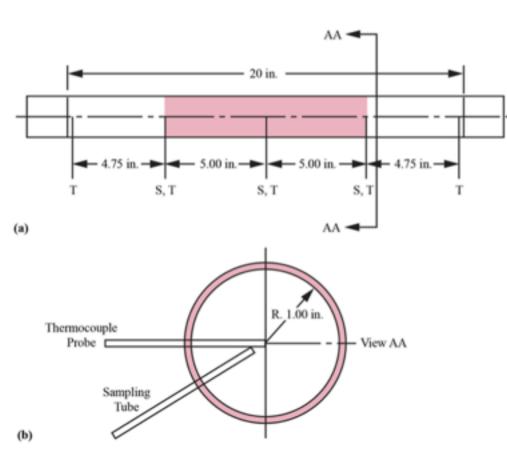
Introduction: Area of Concern

- Execution speed requirements dictate use of simplified one-dimensional model for cyclic process simulations
- * 1-D axially dispersed plug flow equation predominantly used in process simulations based on current literature
- Simplifying assumptions include two lumped mass transfer terms requiring empirical determination
- * Mass transfer term determination is generally via breakthrough analysis in sub-scale fixed-beds with a low tube diameter to particle diameter ratio

$$\frac{\partial c}{\partial t} + \left(\frac{1-\varepsilon}{\varepsilon}\right) \frac{\partial \overline{q}}{\partial t} - D_L \frac{\partial^2 c}{\partial x^2} = -\frac{\partial v_i c}{\partial x}$$

$$\frac{\partial \overline{q}}{\partial t} = k_n (q^* - \overline{q})$$

Introduction: Research Findings (1)

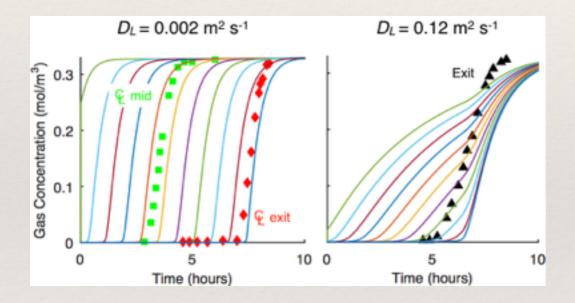


(a) Breakthrough test apparatus and (b) cross-sectional view of a typical temperature measurement and gas sampling location. "T" indicates thermocouple probe location, and "S" indicates sampling tube location. Shading in (a) indicates location of sorbent packing.

- Standard breakthrough analysis is based on measurement taken after mixing of two flow regimes: in the bed core, and channeled flow along the walls
 - Resultant inaccuracies in mass transfer term cause errors during simulation-based design of fullscale separation process
 - An improved approach was developed to use a centerline measurement in addition to the mixed measurement and determine terms individually

Knox, J. C. Finite Difference Modeling and Experimental Investigation of Carbon Dioxide Adsorption on a Molecular Sieve Sorbent Material Used in Spacecraft Carbon Dioxide Removal Systems : A Thesis. University of Alabama, Huntsville, 1992.

Introduction: Research Findings (2)



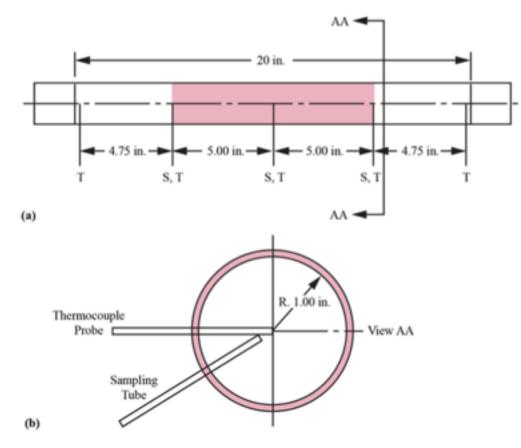
Knox, J. C.; Ebner, A. D.; LeVan, M. D.; Coker, R. F.; Ritter, J. A., Limitations of Breakthrough Curve Analysis in Fixed-Bed Adsorption. *Ind Eng Chem Res* **2016**.

- Axial dispersion term derived based on Fickian (molecular) diffusion, but is used to model dispersion arising from flow around pellets and wall effects
 - For strongly adsorbed species, interaction of a large dispersion term with the ill-posed Danckwerts boundary condition causes hidden nonphysical simulation result
 - * To prevent nonphysical behavior, limiting expressions for the mass transfer terms were derived for specific sorbent/sorbate pairs and inlet conditions
 - A generalized expression was derived to limit the mass transfer terms for any sorbent/sorbate pair based on the strength of adsorption

Principle Equations in 1-D Model

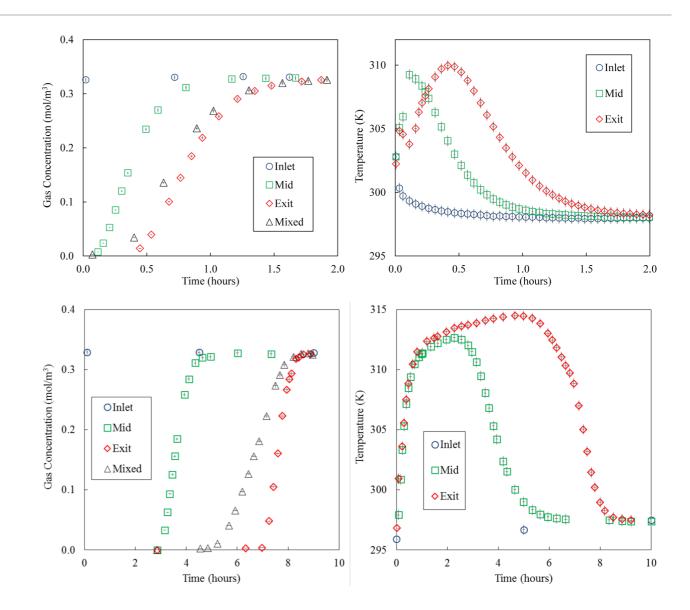
All variables in Mass and Heat Balance Equations are determined except D_L, k_n, and h_o

Experimental Results



(a) Breakthrough test apparatus and (b) cross-sectional view of a typical temperature measurement and gas sampling location. "T" indicates thermocouple probe location, and "S" indicates sampling tube location. Shading in (a) indicates location of sorbent packing.

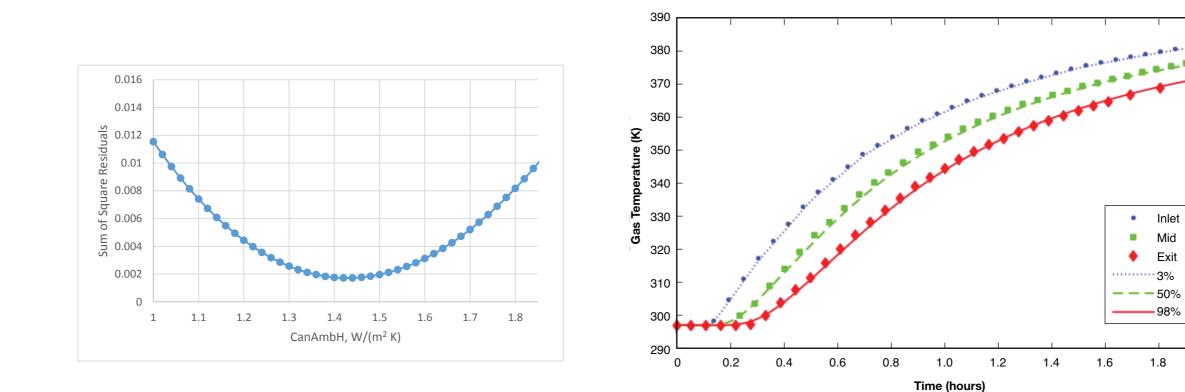
Knox, J. C. Finite Difference Modeling and Experimental Investigation of Carbon Dioxide Adsorption on a Molecular Sieve Sorbent Material Used in Spacecraft Carbon Dioxide Removal Systems : A Thesis. University of Alabama, Huntsville, 1992.



Left panels: Experimental gas-phase concentration profile history breakthrough curves for CO2 (top) and H2O vapor (bottom) on zeolite 5A at 3 centerline locations in the bed (circles: 2.5%, squares: 50%, and diamonds: 97.5%) and just outside the bed (triangles). Right panels: Corresponding experimental temperature profile histories for CO2 (top) and H2O vapor (bottom) on zeolite 5A at 3 centerline locations in the bed (circles: 2%, squares: 50%, and diamonds: 98%). Error bars show experimental uncertainty.

Knox, J. C.; Ebner, A. D.; LeVan, M. D.; Coker, R. F.; Ritter, J. A., Limitations of Breakthrough Curve Analysis in Fixed-Bed Adsorption. *Ind Eng Chem Res* **2016**.

Step 1: Wall to Ambient Heat Transfer Coefficient



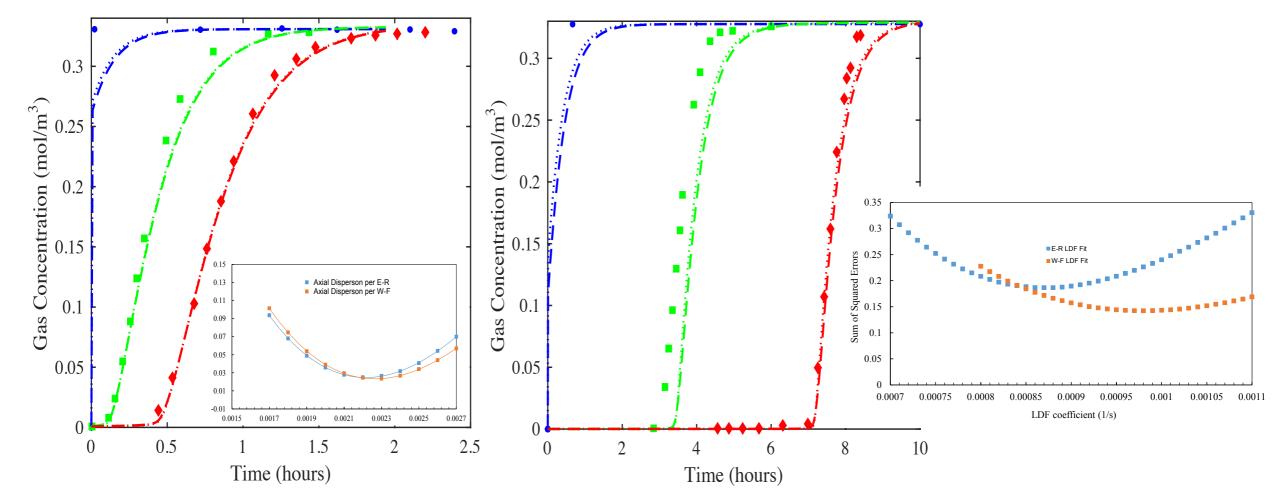
Sum of Square Residuals for Experimental and Simulation Data

Temperature history data for the thermal characterization test with N₂

2

*h*_o is empirically derived via a Thermal Characterization Test

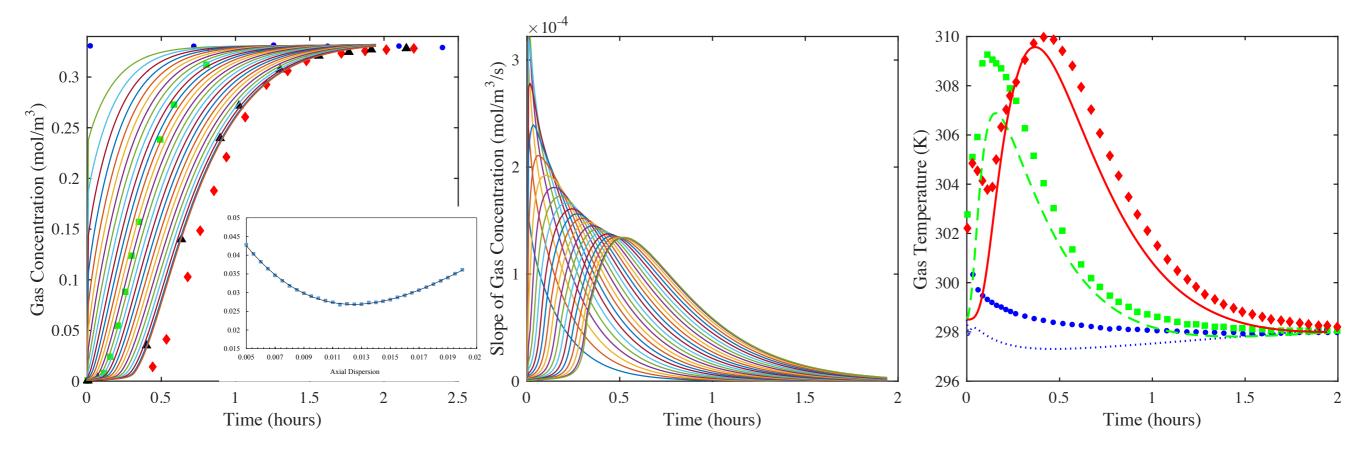
Step 2: Linear Driving Force Mass Transfer Coefficient



Fits of the 1-D axial dispersed plug flow model to the 97.5% location (diamonds) experimental centerline gas-phase concentration breakthrough curves for CO₂ (left) and H₂O vapor (right) on zeolite 5A, and corresponding predictions from the model of the 2.5% (circles) and 50% (squares) locations. The saturation term in the CO₂-zeolite 5A isotherm was increased by 15%. The saturation term in the H₂O vapor-zeolite 5A isotherm was decreased by 3%. The void fraction was reduced to 0.33 based on the Cheng distribution (Cheng *et al.*, 1991) with C = 1.4 and N = 5, as recommended by Nield and Bejan (1992)

 k_n is empirically derived via fitting to centerline concentration breakthrough curve. For this step, dispersion is taken to result from pellet effects only (no wall effects). Choice of dispersion correlation has a small impact on k_n

Step 3: Axial Dispersion Coefficient (CO₂ Case)

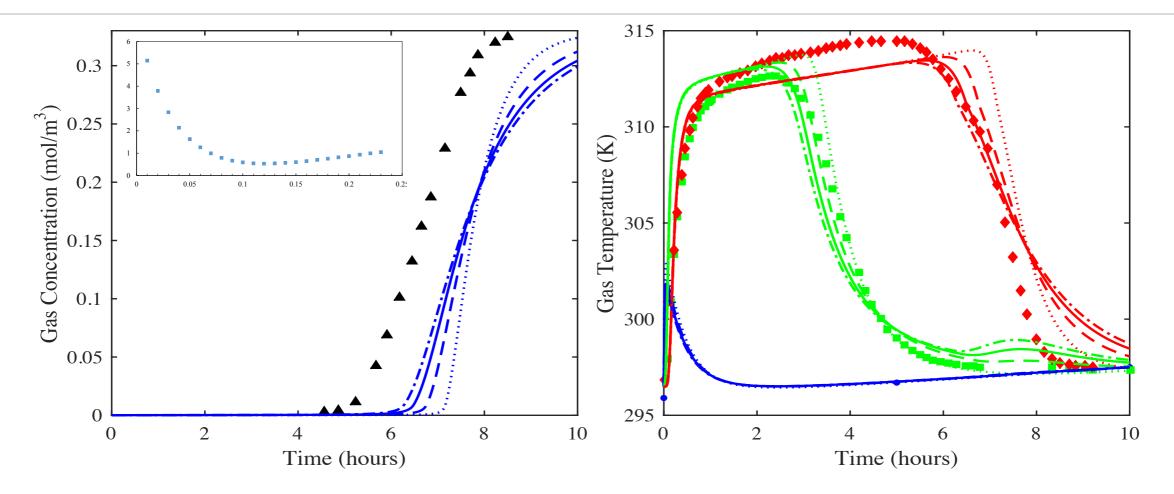


 CO_2 on zeolite 5A: Fit of the 1-D axial dispersed plug flow model to the outside bed (triangles) experimental breakthrough curve using a value of D_L 7 times greater than that from the Wakao and Funzzkri correlation and the fitted LDF $k_n = 0.0023 \text{ s}^{-1}$ (left panel). The reported saturation term for the CO_2 -zeolite 5A isotherm was used, along with **the reported void fraction of 0.35**. Predictions from the model (lines) of the gas-phase concentration breakthrough curves at 0, 4, 8, 12, ..., 92, 96 and 100% locations in the bed are also shown in the left panel, along with the 2.5% (circles), 50% (squares) and 97.5% location (diamonds) experimental center line gas-phase concentration breakthrough curves in the bed are shown in the middle panel. Predictions from the model (lines) of the 2.5% (squares) and 97.5% location (diamonds) experimental center line temperature profile histories are shown in the right panel.

 D_L term is fit to mixed gas concentration (far downstream), but requires value 7 times the correlation value to compensate for wall channeling. Fit is specific to the size of the column; for a much larger column wall channeling may be neglected and correlated values of D_L used (but not for fixed beds with a tube to pellet ratio of 20 as in this

case, or less)

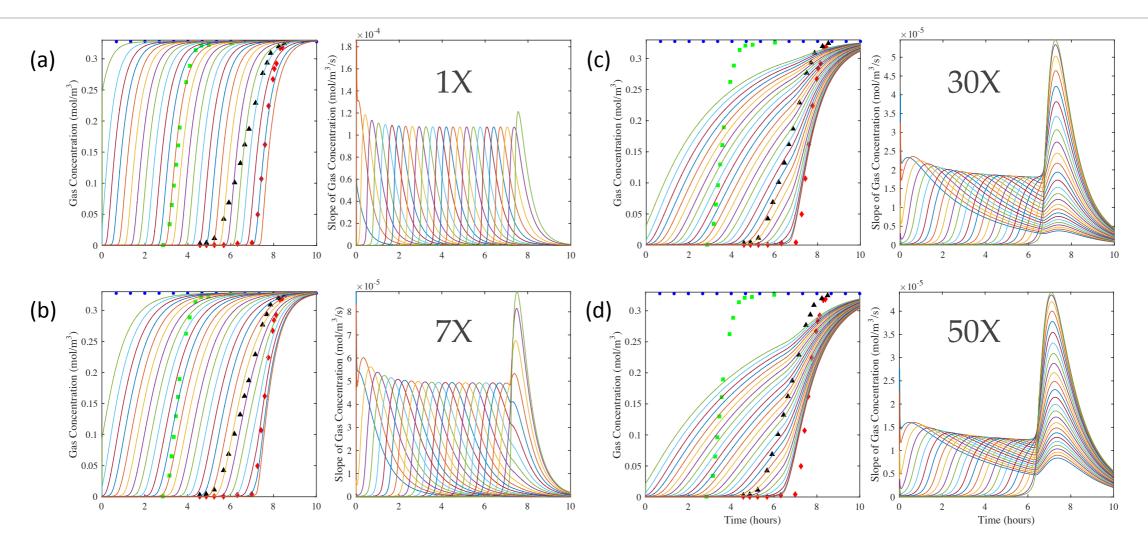
Step 3: Axial Dispersion Coefficient (H₂O Case)



H₂O vapor on zeolite 5A: Predictions from the 1-D axial dispersed plug flow model of the outside the bed (triangles) experimental breakthrough curve when varying the value of D_L . $D_L = 10$ (dotted lines), 30 (dashed lines), 50 (solid lines) and 70 (dash-dot lines) times greater than Wakao and Funzkri correlation with the LDF $k_n = 0.00083 \text{ s}^{-1}$ (left panel). The reported saturation term for the H₂O-zeolite 5A isotherm was used, along with the reported void fraction of 0.35. The corresponding predictions from the model (lines) of the 2.5% (circles), 50% (squares) and 97.5% location (diamonds) experimental center line temperature profile histories are shown in the right panel.

 D_L term is fit to mixed gas concentration (far downstream), but requires value 50(!) times the correlation value to compensate for wall channeling. However the temperature profiles deviate increasingly from the test data with increasing D_L indicating a breakdown of the axial dispersed plug flow model.

Step 3: Axial Dispersion Coefficient (H₂O Case)



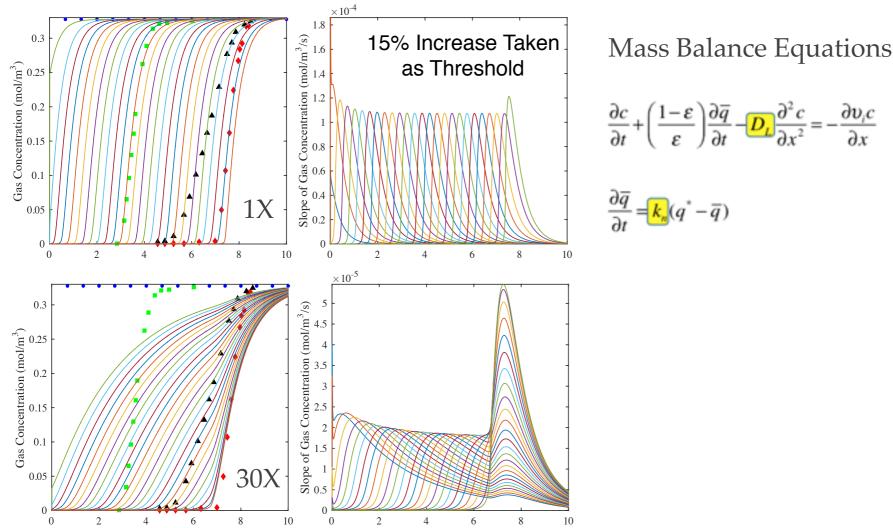
H₂O vapor on zeolite 5A: Predictions from the model (lines) shown in Figure 9 of the gas-phase concentration breakthrough curves at 0, 4, 8, 12, ..., 92, 96 and 100% locations in the bed (left panels). The 2.5% (circles), 50% (squares) and 97.5% location (diamonds) experimental centerline gas-phase concentration breakthrough curves are also shown for comparison in the left panels. The corresponding derivatives (or slopes) of the gas-phase concentration breakthrough curves in the bed are shown in the right panels. (a) D_L = Wakao-Funazkri correlation, and (b) D_L = 7, (c) 30 and (d) 50 times greater than Wakao and Funazkri correlation.

At 7X, internal concentration history slope matches mixed concentration just as for CO₂ case. This indicates that same dispersive mechanism occurs regardless of sorbate. To overcome non-physical breakthrough sharpening, *D_L* must be increased by 50X to decrease breakthrough slope. Expected CPB is lost entirely for this condition.

Modeling Conclusions

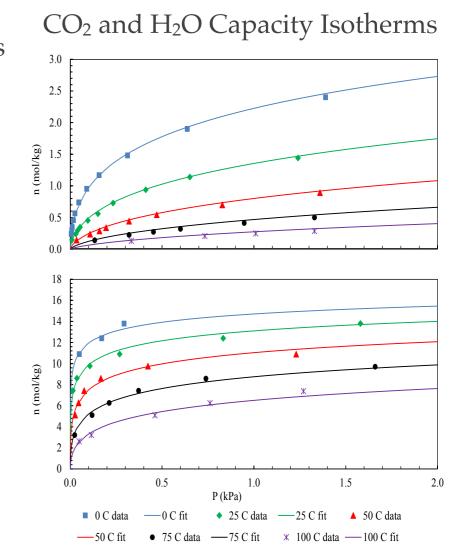
- Breakthrough tests with tube diameter to pellet diameter ratios of around 20 (or less), are subject to wall channeling, an mechanism not captured in standard dispersive correlations. Breakthrough tests are generally sub-scale to conserve sorbent materials and gas flow equipment costs and thus frequently in this range.
- * The typical breakthrough measurement is taken far downstream, after mixing. Fitting the mass transfer coefficient to this measurement will provide erroneous results for a larger (or smaller) diameter column due to the influence of channeling.
- * A method has been demonstrated where a centerline measurement is used to derive a mass transfer coefficient that captures physics free of wall effects and thus appropriate for scale-up to large diameter columns.
- Using the mass transfer coefficient derived above, this method uses the mixed concentration data for fitting of a dispersion coefficient D_L specific to the tube diameter, as needed for processes that utilize small diameter tubes.
- However fitting D_L blindly to the breakthrough curve (as apparent in many published breakthrough analyses) can, in specific cases, result in a complete breakdown of the axially dispersed plug flow model, and result in fitted coefficients that are incorrect.
- * Thus it is important to map the set of conditions where significant breakthrough sharpening occurs in order to avoid nonphysical and non-predictive simulation behavior.

Mapping the Sensitivity of Sorbate/Sorbent Systems to D_L and k_n



Slope ratio provides metric for breakthrough sharpening and departure from constant pattern behavior

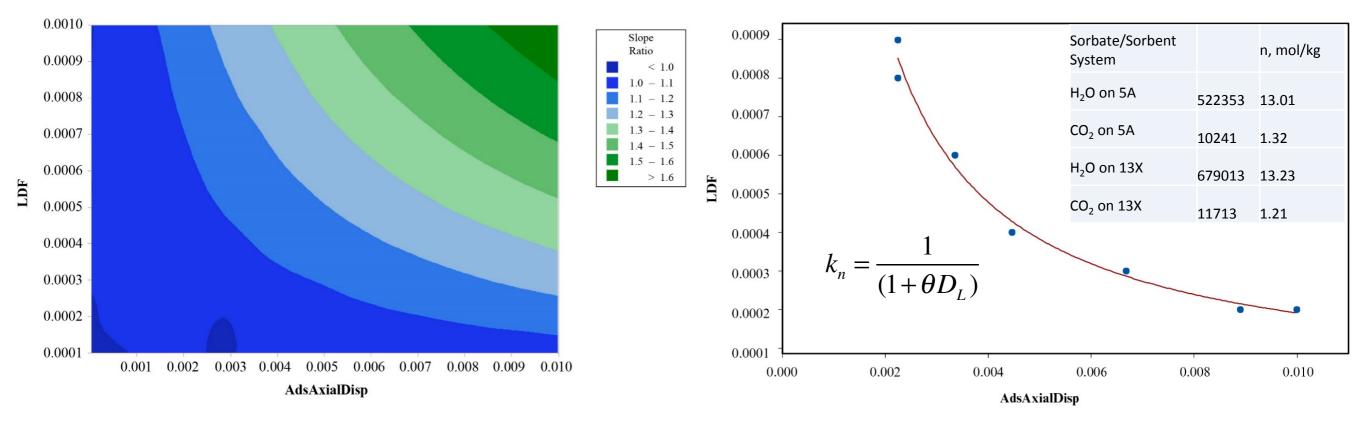
 $\frac{\partial c}{\partial t} + \left(\frac{1-\varepsilon}{\varepsilon}\right) \frac{\partial \overline{q}}{\partial t} - \frac{D_L}{\partial x^2} \frac{\partial^2 c}{\partial x^2} = -\frac{\partial v_i c}{\partial x}$



Equilibrium adsorption isotherms for CO2 (top) and H2O vapor (bottom) on zeolite 5A at temperatures from 0°C to 100°C as indicated. Symbols represent experimental data; Toth isotherm fits are shown as lines (Wang and LeVan, 2009)

$$n = \frac{ap}{\left[1 + (bp)^{t}\right]^{1/t}}; \quad b = b_{0} \exp(E/T); \quad a = a_{0} \exp(E/T); \quad t = t_{0} + c/T$$

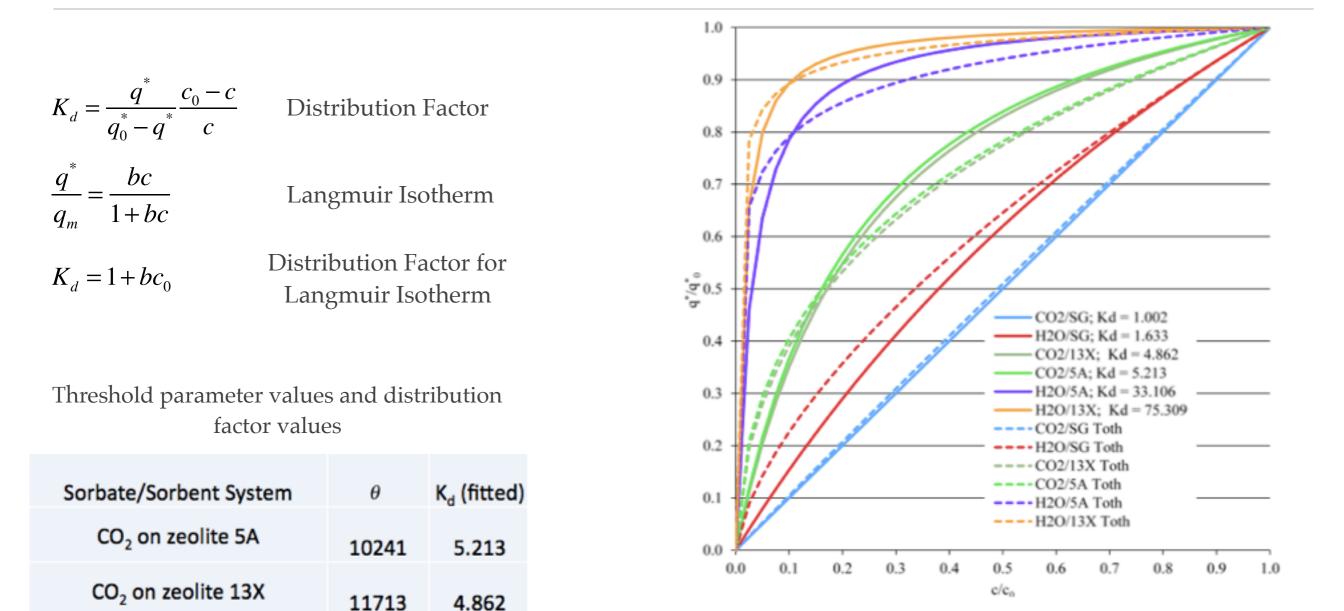
Threshold parameter determination for H_2O on 5A (similar analysis for CO_2 on 5A, H_2O on 13X, and CO_2 on 13X)



Contour plot of slope ratio for H₂O/5A system based on 100 breakthrough simulations Curve fit of $k_n = f(D_L)$ for simulation runs with slope ratio values between 1.13 and 1.16 for H₂O on 5A. Coefficient of determination (R²) is 0.998.

For this system, the simulation will result in a slope ratio limit below the threshold if $k_n(1+\theta D_L)-1<0$

Generalization to any sorbent/sorbate system



17

4.862

33.106

75.309

522353

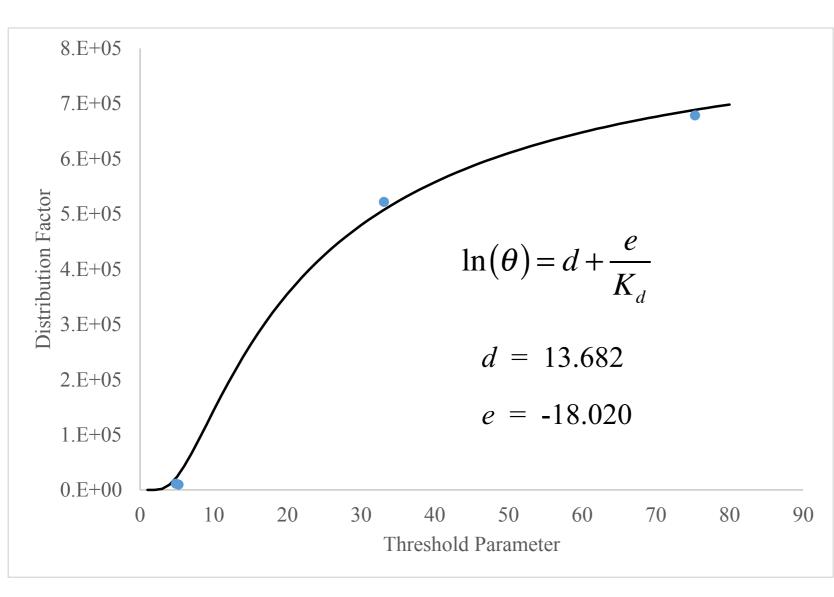
679013

H₂O on zeolite 5A

H₂O on zeolite 13X

Normalized concentration vs. normalized bed loading for six sorbate/sorbent systems for conditions of 10°C and 1.0 kPa. Solid lines: Langmuir isotherms; Dashed lines: Toth isotherms.

Correlation between threshold parameter and distribution factor



Threshold parameter values and distribution factor values

Sorbate/Sorbent System	θ	K _d (fitted)
CO ₂ on zeolite 5A	10241	5.213
CO ₂ on zeolite 13X	11713	4.862
H ₂ O on zeolite 5A	522353	33.106
H ₂ O on zeolite 13X	679013	75.309

Estimated threshold value q vs. distribution factor Kd for four sorbate/ sorbent systems (filled circles) and fitted relationship shown in Equation 5.6 (line). Coefficient of determination (R²) is 0.997.

Three-step process to prevent excessive breakthrough sharpening

- 1. Determine distribution factor (K_d) for sorbent/sorbate system of interest by fitting to Langmuir isotherm
- 2. Calculate threshold parameter:

 $\ln(\theta) = d + \frac{e}{K_d}$

3. Map limits on D_L vs. k_n plot based on: $k_n = \frac{1}{(1 + \theta D_L)}$

For values where $k_n(1+\theta D_L)-1<0$ excessive breakthrough sharpening and breakdown of the constant pattern behavior will be avoided

Conclusions for Parameter Mapping

- The axially dispersed plug flow equation and the Danckwerts boundary condition works well for values of dispersion within bounds of accepted correlations
- * However, for specific combinations of K_d, D_L and k_n this model breaks down due to the elimination of dispersion at the outlet boundary. In these cases, significant breakthrough sharpening occurs as well as distortion of the internal concentration, deviating from the accepted CPB for these systems.
- * This work present a methodology where a threshold parameter may be calculated based on *K*_d, *D*_L and *k*_n, and applied to avoid non-physical model distortion

Overall Conclusions

- * The separation of gases through adsorption plays an important role in the chemical processing industry, where the separation step is often the costliest part of a chemical process and thus worthy of careful study and optimization.
- * This work developed a number of new, archival aspects on the computer simulations used for the refinement and design of these gas adsorption processes:
 - 1. Presented a new approach to fit the undetermined heat and mass transfer coefficients in the axially dispersed plug flow equation and associated balance equations
 - 2. Examined and described the conditions where non-physical simulation results can arise
 - 3. Presented an approach to determine the limits of the axial dispersion and LDF mass transfer terms above which non-physical simulation results occur



Gas Separation Processes

- Separation processes are defined as those that transform a mixture of substances into two or more product streams (King, 1980)
- The study of separations is of critical importance as they are the costliest step in many chemical processes, as they reverse the mixing of substances and thus require a decrease in entropy (Yang 2003)

Table 2.1 Common Commercial and Industrial Uses for Sorbents (Keller, 1983; Yang, 2003)

Component to be adsorbed	Other components	Adsorbent(s)			
Gas purification					
H ₂ O	Olefin-containing cracked gas, natural gas, air, synthesis gas, etc.	Silica, alumina, zeolite (3A)			
CO ₂	C ₂ H ₄ , natural gas, etc.	Zeolite, carbon molecular sieve			
Hydrocarbons, halogenated organics, solvents	Vent streams	Activated carbon, silicalite, others			
Sulfur compounds	natural gas, hydrogen, liquefied petroleum gas (LPG)	Zeolite, activated alumina			
SO ₂	Vent streams	Zeolite, activated carbon			
Gas bulk separations					
Normal paraffins	iso-paraffins, aromatics	Zeolite			
N ₂	O ₂	Zeolite			
O ₂	N ₂	Carbon molecular sieve			
со	CH4, CO2, N2, Ar, NH3/H2	Zeolite, activated carbon			
Acetone	Vent streams	Activated Carbon			
C ₂ H ₄	Vent streams	Activated Carbon			

2003)	pplications Enabled by New Sorbents (1 ang,
Application	Sorbent and Notes

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- ipplication	Soroeni alla riotes
N ₂ /CH ₄ separation for natural gas upgrading	Clinoptilolite, tinanosilicates by kinetic separation, single-wall carbon nanotubes
CO removal from H2 to < 1 ppm for fuel cell applications	π -complexation sorbents such as CuCl/ γ - Al ₂ O ₃ , CuY, and, AgY
NOxremoval	Fe-Mn-Ti oxides, Fe-Mn-Zr oxides, Cu- Mn oxides, multi-wall carbon nanotubes
C ₃ H ₆ /C ₃ H ₈ (+hydrocarbons) separation	π-complexation sorbents such as CuCl/γ- Al ₂ O ₃ , AgNO3/SiO2, AgNO3/clays, aluminophosphate
C2H6/C2H6 (+hydrocarbons) separation	π-complexation sorbents such as CuCl/γ- Al ₂ O ₃ , AgNO3/SiO2, AgNO3/clays

Table 2.3 CO₂ Capture Technologies Funded Under DOE (Vora, 2013).

Project Name	Project Focus	Sorbent Materials	Process Approach	Technology Maturity	Ref.
Bench-Scale Development & Testing of a Novel Adsorption Process for Post- Combustion CO2 Capture	Novel Adsorption Process	Micro- porous carbon	TSA, fixed-beds	Bench-Scale, Actual Flue Gas	Jain, 2012
Low-Cost Sorbent for Capturing CO2 Emission Generated by Existing Coal- Fired Power Plants	Low-Cost Solid Sorbent	Alkalized Alumina sorbent	Simulated Moving Beds	Bench-Scale Using Actual Flue Gas	Elliot, 2012
CO2 Removal from Flue Gas Using Microporous Metal Organic Frameworks	Micro- porous MOFs	Alumina and Mg/ DOBDC	VPSA	Laboratory- Scale, Simulated Flue Gas	Benin, 2012

Adsorbents and Fixed Beds

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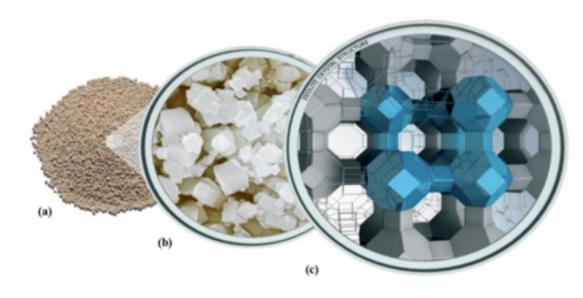


Figure 2.3 (a) Pelletized zeolite pellets, (b) crystals, and (c) framework structure http://www.grace.com/engineeredmaterials/productsandapplications/InsulatingGlass/Siev eBeads/Grades.aspx)

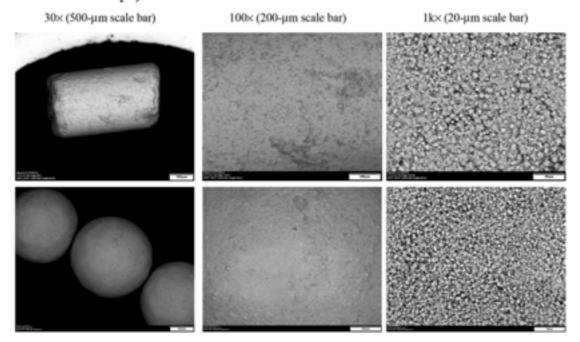
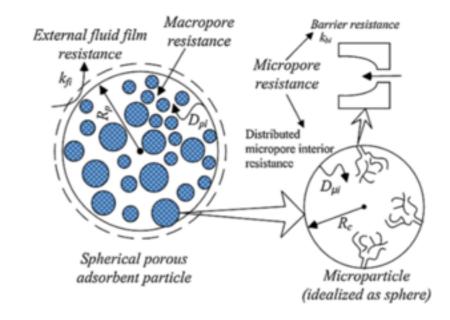


Figure 2.4 SEM images of pelletized zeolite 5A used in the ISS CDRA. Individual zeolite crystals are evident in the 1kx views (Radenburg, 2013).







Literature Review of Fixed Bed Gas Adsorption Models

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	Application	System	mental	Spatial Dimensions		be Particle aweter	1	las to Particle Rate Expression	Method to Determine Gas to Particle Rate	Axial Dispersion	Internal Profile Shown?	Reference
	Post-combustion CO; capture, steam methane reforming	CO ₂ or hydrot and we	alsite (dry	1		14	1	Modified LDF: function of oading and isotherm (pore liffusion model)	Breakthrough analysis (adsorb and desorb)	Estimated per Edwards and Richardson 1968	80	Ding and Alpay 2000
	Hydrogen purification	CO on	D ₁ , CH4, 5A, ted Carbon	1	1	8 and 15	I	DF	Breakthrough analysis (Park et al. 1998)	TODE	BD	Park et al., 2000
	CO ₂ scrubbing	H ₂ O at 5A	nd CO ₂ on	1		20	1	DF	Breakthrough analysis	Estimated per Edwards and Richardson 1968	yes	Mohamadinejad et al., 2000
	Dehumidification of organic solvents	H ₂ O a on 4A	nd Acetone	2		40	1	ii-disperse pellet modeled	Not specified	Breakthrough Analysis	no	Pentchev and Selkova, 2002
	Dehumidification of organic solvents	H2O o 13X	n Silica gel,	1		10	1	DF	Uptake curve analysis (Yang and Lee, 1998)	Estimated per Wakao and Funazkri, 1978	80	Ahn and Lee, 2003
	CO ₂ scrubbing	CO ₂ at 5A	nd H ₂ O on	2		20	L	DF	Breakthrough analysis	Estimated per Edwards and Richardson 1968	Yes (CO ₂ only)	Mohamadinejad et al., 2003
	Drying of instrument air	H ₂ O et	6 4A	I		10	5	dodified LDF as a unction of ressure, temperature and nolar fraction	Breakthrough analysis	none	80	Gorbach et al., 2004
1	Dehumidification of organic solvents		n Silica gel, na, 13X	1		10		DF	Breakthrough analysis (Ahn and Lee, 2003)	Estimated per Wakso and Funazkri, 1978	no	Ahn and Lee, 2004
,	Oxygen purity	O2, At CMS	, and N2 on	1		n/a	0	Modified LDF concentration-dependent liffusivity combined with	Estimated per Bae and Lee (2005)	yes	BD	Jee et al., 2005
10	Post-combustion CO1 ca	pture	CO; and N2 on silicalite)	1		11	LDF	Estimated per Farooq and Rathven 1990	Estimated per Wakao et al., 1978	10	Delgado et al., 2006
11	Gas Separation		CH4 and CO ₂ of 5A, butane and pentane on silicalite		1		8	Double LDF	Estimated per method reported in this paper, adjusted via breakthrough analysis	defined	10	Leinekugel-le- Cocq et al., 2007
12	Hydrogen parification		CO on 5A (4 samples) and A in H2	1C	1	7 at	nd 11	LDF	Breakthrough analysis	Estimated per Lopes et al., 2009	EO	Bastos-Noto et al., 2011
13	Post-combustion CO2 ca	pture	CO ₂ and N2 on 13X	1	1		6	Combined LDF and QDF	Breakthrough analysis	None	No	Won et al., 2012
14	Capture of hydrocarbon emissions from gasoline engines during the cold s period of the engine		Propane on Na ZSM-5	•	1	2	156	LDF	Estimated from film at micropore calculations per Brosillon et al. 200	specified)	Yes	Paertolas et al., 2012
15	Post-combustion CO2 ca	pture	CO; on 13X		1	1	21	Macropore and micropore solved simultaneously	Estimated + breakthrough analysis	Estimated per Wakao and Funazkri, 1978	Yes	Mulgundmath et al., 2012
16	Post-combustion CO2 ca	pture	CO; and N2 on carbon	1	1	9	,3	LDF	Breakthrough analysis and estimated via Ruthven 1984	None	No	Gonzlez et a., 2013
17	Development process of reactor design for open thermochemical energy storage	a	H-O on 13X		2	1	25	LDF	Breakthrough analysis	Yes	Temperatu only	re Mette et al., 2014
18			Ethanol and H ₂ on 3A	0	1		6	LDF	Breakthrough analysis	None	Yes	Kupice et al., 2014
19	Dehumidification of gase containing organic component	cs.	H/O and benze on Silica gel, I activated carbo	3X,	1		o'a	LDF	Breakthrough analysis (Ko et al., 2002, Park and Knaebel 1992, and Ahn and Lee 2003)	Edwards and	No	Nastaj and Ambrozek, 2015

Table A.1 Literature Review of Fixed Bed Gas Adsorption Models

- Criteria for inclusion:
 - Published in 2000 or later
 - Includes description of experimental data used for validation
- 1-D model used in 16 publications
- * Tube to particle diameter ratio \leq 20 for 16 (most much lower)
- LDF used in 12 publications
- Axial dispersion used in 14 publications
- Breakthrough curve only shown in 14 publications